

Phenomenology of Two-Body Radiative B -Meson Decays

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Based on the papers by

A. Ali and A.P., Eur. Phys. J. **C23** (2002) 89 [hep-ph/0105302]

A. Ali, E. Lunghi, and A.P., Phys. Lett. **B595** (2004) 323
[hep-ph/0405075]

A. Ali and A.P., hep-ph/0610149

Introduction

- Interest in $B \rightarrow (\rho, \omega) \gamma$ decays is motivated by their potential importance for getting information on the CKM matrix, in particular, to extract $|V_{td}|$ and UT angle α
- Contributions from tree and penguin operators are of comparable size in the decay amplitude and differ by a weak phase, so both branching fractions and different asymmetries are sensitive to the CKM matrix elements
- Different approaches have been applied for the analysis of $B \rightarrow V \gamma$ decays: QCD Factorization, Perturbative QCD approach, SCET Factorization, etc.
- Application of QCD Factorization to the $B \rightarrow V \gamma$ decays and comparison of results with existing experimental data is the main topic of this talk

Effective Electroweak Theory

- Weak interactions at energies $E \ll M_W, M_Z$ are most conveniently described by **an effective theory**
- This theory is derived from the SM by integrating out heavy particles – top quark, W - and Z -bosons, Higgs
- Lagrangian density includes all the other quark flavors

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QCD} \times \text{QED}} + \mathcal{L}_{\text{weak}}^{b \rightarrow d} + \mathcal{L}_{\text{weak}}^{b \rightarrow s}$$

- Flavor-changing neutral current (FCNC) term $\mathcal{L}_{\text{weak}}^{b \rightarrow d}$ describes $b \rightarrow d$ transition

$$\mathcal{L}_{\text{weak}}^{b \rightarrow d} = -\frac{G_F}{\sqrt{2}} \sum_{p=u,c} \lambda_p^{(d)} \sum_j C_j(\mu) \mathcal{O}_j(\mu)$$

- $\mathcal{L}_{\text{weak}}^{b \rightarrow s}$ for $b \rightarrow s$ transition can be obtained from $\mathcal{L}_{\text{weak}}^{b \rightarrow d}$:
 1. $d \rightarrow s$ for the quark fields in all the operators $\mathcal{O}_j(\mu)$
 2. $\lambda_d^{(p)} \equiv V_{pb} V_{pd}^* \rightarrow \lambda_s^{(p)} \equiv V_{pb} V_{ps}^*$ in the CKM factors

$B \rightarrow V$ Transition Form Factors

General decomposition on Lorentz structures admits **seven** form factors of the momentum squared $q^2 = (P - p)^2$

$$\langle V(p, \varepsilon^*) | \bar{Q} \gamma^\mu b | \bar{B}(P) \rangle = \frac{2i V^{(V)}(q^2)}{M + m_V} \epsilon^{\mu\nu\rho\sigma} \varepsilon_\nu^* p_\rho P_\sigma$$

$$\begin{aligned} \langle V(p, \varepsilon^*) | \bar{Q} \gamma^\mu \gamma_5 b | \bar{B}(P) \rangle &= A_1^{(V)}(q^2) (M + m_V) \left[\varepsilon^{*\mu} - \frac{(\varepsilon^* q)}{q^2} q^\mu \right] \\ &\quad - A_2^{(V)}(q^2) \frac{(\varepsilon^* q)}{M + m_V} \left[P^\mu + p^\mu - \frac{M^2 - m_V^2}{q^2} q^\mu \right] + 2m_V A_0^{(V)}(q^2) \frac{(\varepsilon^* q)}{q^2} q^\mu \end{aligned}$$

$$\langle V(p, \varepsilon^*) | \bar{Q} \sigma^{\mu\nu} q_\nu b | \bar{B}(P) \rangle = 2 T_1^{(V)}(q^2) \epsilon^{\mu\nu\rho\sigma} \varepsilon_\nu^* p_\rho P_\sigma$$

$$\begin{aligned} \langle V(p, \varepsilon^*) | \bar{Q} \sigma^{\mu\nu} \gamma_5 q_\nu b | \bar{B}(P) \rangle &= -i T_2^{(V)}(q^2) [(M^2 - m_V^2) \varepsilon^{*\mu} - (\varepsilon^* q) (P + p)^\mu] \\ &\quad - i T_3^{(V)}(q^2) (\varepsilon^* q) \left[q^\mu - \frac{q^2}{M^2 - m_V^2} (P + p)^\mu \right] \end{aligned}$$

Symmetry Relations in $B \rightarrow V$ Transitions

- The **heavy quark symmetry** and the **large recoil limit** of the final state meson allow the form-factors' reductions
- Neglecting terms $\sim m_V^2/M^2$, relations at $q^2 = 0$:

$$\frac{M}{M+m_V} V^{(V)}(0) = \frac{M+m_V}{M} A_1^{(V)}(0) = T_1^{(V)}(0) = T_2^{(V)}(0) = \xi_{\perp}^{(V)}(0)$$

$$\frac{2m_V}{M} A_0^{(V)}(0) = \frac{M+m_V}{M} A_1^{(V)}(0) - \frac{M-m_V}{M} A_2^{(V)}(0) = T_2^{(V)}(0) - T_3^{(V)}(0) = \xi_{\parallel}^{(V)}(0)$$

- Valid for **soft contributions** (neglecting corrections $\sim 1/M$ and $\sim \alpha_s$)
- Factorization scheme is required (“soft form factors” renormalization conventions); holds **exactly** to all orders in perturbation theory

$$V^{(V)}(0) \equiv \frac{M+m_V}{M} \xi_{\perp}^{(V)}(0) \quad A_0^{(V)}(0) \equiv \frac{M}{2m_V} \xi_{\parallel}^{(V)}(0)$$

$B \rightarrow K^* \gamma$ Branching Fraction in LO

- In the leading order, the penguin operator $\mathcal{O}_{7\gamma}$ contributes only

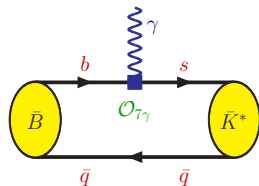
- Form-factor symmetry relation:

$$T_1^{(K^*)}(0) = T_2^{(K^*)}(0)$$

- Branching fraction

$$B_{\text{th}}^{\text{LO}}(B \rightarrow K^* \gamma) = \tau_B \frac{G_F^2 |V_{tb} V_{ts}^*|^2 \alpha M^3}{32\pi^4} \bar{m}_b^2(\mu_b) |C_7^{(0)\text{eff}}(\mu_b)|^2 |T_1^{(K^*)}(0, \mu_b)|^2$$

- The b -quark mass $\bar{m}_b(\mu_b)$ and Wilson coefficient $C_7^{(0)\text{eff}}(\mu_b)$ are dependent on the scale $\mu_b = \mathcal{O}(m_b)$; to compensate it, one should assume μ_b -dependence in $T_1^{(K^*)}(0, \mu_b)$



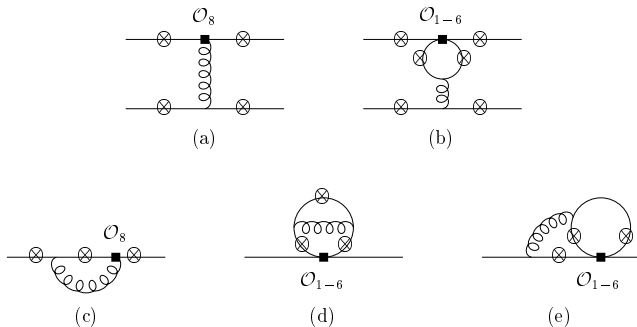
$B \rightarrow K^* \gamma$ Branching Fraction in NLO

$$\mathcal{B}_{\text{th}}(B \rightarrow K^* \gamma) = \tau_B \frac{G_F^2 \alpha |V_{tb} V_{ts}^*|^2}{32 \pi^4} m_{b,\text{pole}}^2 M^3 \left[\xi_{\perp}^{(K^*)}(0) \right]^2 \left| C_7^{(0)\text{eff}}(\mu) + A^{(1)}(\mu) \right|^2$$

The function $A^{(1)}(\mu)$ includes all the NLO corrections

$$A^{(1)}(\mu) = A_{C_7}^{(1)}(\mu) + A_{\text{ver}}^{(1)}(\mu) + A_{\text{sp}}^{(1)K^*}(\mu_{\text{sp}})$$

- $A_{C_7}^{(1)}(\mu) - \mathcal{O}(\alpha_s)$ corrections from Wilson coefficient $C_7^{\text{eff}}(\mu)$ and $\bar{m}_b(\mu)$
- $A_{\text{ver}}^{(1)}(\mu) - \mathcal{O}(\alpha_s)$ correction to the $b \rightarrow s \gamma$ vertex
- $A_{\text{sp}}^{(1)K^*}(\mu_{\text{sp}}) - \mathcal{O}(\alpha_s)$ hard-spectator contribution evaluated at intermediate scale $\mu_{\text{sp}} = \sqrt{\mu \Lambda_H}$ with $\Lambda_H \simeq 0.5 \text{ GeV}$

Nonfactorizable α_s Corrections

- First line: hard-spectator corrections
- Second line: $b \rightarrow s \gamma$ vertex corrections

Phenomenological Evaluation of $\xi_{\perp}^{(K^*)}(0)$

- $\mathcal{B}(B^+ \rightarrow K^{*+} \gamma)$ $\xi_{\perp}^{(K^*)}(0) = 0.286 \pm 0.025$

- $\mathcal{B}(B^0 \rightarrow K^{*0} \gamma)$ $\xi_{\perp}^{(K^*)}(0) = 0.291 \pm 0.024$

Average $\bar{\xi}_{\perp}^{(K^*)}(0) = 0.289 \pm 0.025$

Full QCD form factor

$$T_1^{(K^*)}(0, \mu) = \xi_{\perp}^{(K^*)}(0) \left\{ 1 + \frac{\alpha_s(\mu)}{4\pi} C_F \left[\ln \frac{m_b^2}{\mu^2} - 1 \right] \right\} + \frac{\alpha_s(\mu_{\text{sp}})}{8\pi} C_F \Delta F_{\perp}^{(V)}(\mu_{\text{sp}})$$

$$\bar{T}_1^{(K^*)}(0, \bar{m}_b) \simeq 1.05 \bar{\xi}_{\perp}^{(K^*)}(0) = 0.303 \pm 0.026$$

LCSR $\bar{T}_1^{(K^*)}(0) = 0.31 \pm 0.04$ [Ball, Jones & Zwicky (2007)]

$B \rightarrow (\rho, \omega) \gamma$ Branching Fraction in NLO

- Charged-conjugate averaged branching ratio in the NLO

$$\begin{aligned} \bar{\mathcal{B}}_{\text{th}}(B^\pm \rightarrow \rho^\pm \gamma) &= \tau_{B^\pm} \frac{G_F^2 \alpha}{32\pi^4} |V_{tb} V_{td}^*|^2 m_{b,\text{pole}}^2 M^3 \left[\xi_\perp^{(\rho)}(0) \right]^2 \\ &\times \left\{ (C_7^{(0)\text{eff}} + A_R^{(1)t})^2 + (F_1^2 + F_2^2) (A_R^u + L_R^u)^2 \right. \\ &\left. + 2F_1 [C_7^{(0)\text{eff}} (A_R^u + L_R^u) + A_R^{(1)t} L_R^u] \right\} \end{aligned}$$

- In CKM elements' ratio, $F_1 \propto \cos \alpha \simeq 0$ for $\alpha \simeq 90^\circ$

$$V_{ub} V_{ud}^* / V_{tb} V_{td}^* = F_1 + iF_2 = -(R_u/R_t) e^{i\alpha}$$

- Amplitude $A^{(1)t}(\mu) = A_{C_7}^{(1)}(\mu) + A_{\text{ver}}^{(1)}(\mu) + A_{\text{sp}}^{(1)\rho}(\mu_{\text{sp}})$
- The u -quark contribution $A^u(\mu) = A_{\text{ver}}^u(\mu) + A_{\text{sp}}^u(\mu_{\text{sp}})$ from penguins can no longer be ignored
- Annihilation contributions $L_R^u = \epsilon_A C_7^{(0)\text{eff}}$; counts as Λ_{QCD}/m_b in the heavy-quark limit

$B \rightarrow (\rho, \omega) \gamma$ Branching Fractions

- Ratio of $B \rightarrow \rho \gamma$ ($B \rightarrow \omega \gamma$) and $B \rightarrow K^* \gamma$ decay widths is preferable; normalized by the experimental value of $B \rightarrow K^* \gamma$ branching fraction

$$\frac{\overline{B}_{\text{th}}(B \rightarrow \rho(\omega) \gamma)}{\overline{B}_{\text{th}}(B \rightarrow K^* \gamma)} = S_{\rho(\omega)} \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{(M^2 - m_{\rho(\omega)}^2)^3}{(M^2 - m_{K^*}^2)^3} \zeta_{\rho(\omega)}^2 [1 + \Delta R(\rho(\omega)/K^*)]$$

- Factors: $S_{\rho^\pm} = 1$; $S_{\rho^0} = 1/2$; $S_\omega = 1/2$
- ζ_ρ and ζ_ω are ratios of Effective theory form factors; in $SU(3)_F$ -symmetry limit, $\zeta_\rho = 1$ and $\zeta_\omega = 1$
- $SU(3)_F$ -breaking effects in QCD form factors $T_1^{(K^*)}(0)$, $T_1^{(\rho)}(0)$, and $T_1^{(\omega)}(0)$ evaluated within the QCD sum-rules

$$\zeta_\rho = \frac{T_1^{(\rho)}(0)}{T_1^{(K^*)}(0)} \simeq \frac{\xi_\perp^{(\rho)}(0)}{\xi_\perp^{(K^*)}(0)} = 0.86 \pm 0.07; \quad \zeta_\omega = \frac{T_1^{(\omega)}(0)}{T_1^{(K^*)}(0)} \simeq \frac{\xi_\perp^{(\omega)}(0)}{\xi_\perp^{(K^*)}(0)} = 0.77 \pm 0.06$$

$B \rightarrow (\rho, \omega) \gamma$ Branching Fractions

- Ratio of CKM matrix elements from CKM unitarity

$$|V_{td}/V_{ts}| = 0.2061 \pm 0.0012^{+0.0080}_{-0.0060} \quad [\text{PDG, 2011}]$$

- Branching ratios (in units of 10^{-6})

$$\bar{B}_{\text{th}}(B^\pm \rightarrow \rho^\pm \gamma) = 1.52 \pm 0.29[\text{th}] \pm 0.06[\text{exp}]$$

$$\bar{B}_{\text{th}}(B^0 \rightarrow \rho^0 \gamma) = 0.72 \pm 0.14[\text{th}] \pm 0.03[\text{exp}]$$

$$\bar{B}_{\text{th}}(B^0 \rightarrow \omega \gamma) = 0.58 \pm 0.11[\text{th}] \pm 0.02[\text{exp}]$$

Mode	BABAR (465 M)	BELLE (657 M)	Average [PDG]
$B^+ \rightarrow \rho^+ \gamma$	$1.20^{+0.42}_{-0.37} \pm 0.20$	$0.87^{+0.29+0.09}_{-0.27-0.11}$	0.98 ± 0.25
$B^0 \rightarrow \rho^0 \gamma$	$0.97^{+0.24}_{-0.24} \pm 0.06$	$0.78^{+0.17+0.09}_{-0.16-0.10}$	0.86 ± 0.15
$B^0 \rightarrow \omega \gamma$	$0.50^{+0.27}_{-0.23} \pm 0.09$	$0.40^{+0.19}_{-0.17} \pm 0.13$	$0.44^{+0.18}_{-0.16}$

- Data and SM are in agreement, but not precisely so due to statistics

Direct CP-Asymmetry

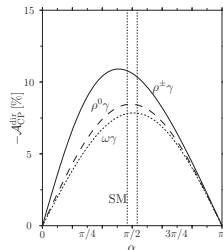
- Direct CP-asymmetry in the $B^\pm \rightarrow \rho^\pm \gamma$ decay rates

$$\mathcal{A}_{\text{CP}}(\rho^\pm \gamma) = \frac{\mathcal{B}(B^- \rightarrow \rho^- \gamma) - \mathcal{B}(B^+ \rightarrow \rho^+ \gamma)}{\mathcal{B}(B^- \rightarrow \rho^- \gamma) + \mathcal{B}(B^+ \rightarrow \rho^+ \gamma)}$$

- Similar definitions in other two modes

$$B^0 \rightarrow \rho^0 \gamma \text{ and } B^0 \rightarrow \omega \gamma$$

- CP-asymmetry arises from interference of penguin operator $\mathcal{O}_{7\gamma}$ and four-quark operators \mathcal{O}_1 and \mathcal{O}_2



- Angle α known precisely $\alpha = (90.0 \pm 5.0)^\circ$ [PDG, 2010]

Mode	SM Pred.	Belle (657M)
$B^\pm \rightarrow \rho^\pm \gamma$	$(-10.6 \pm 2.8)\%$	$(-11 \pm 32 \pm 9)\%$
$B^0 \rightarrow \rho^0 \gamma$	$(-8.5^{+3.7}_{-3.4})\%$	$(-44 \pm 49 \pm 14)\%$
$B^0 \rightarrow \omega \gamma$	$(-7.9^{+3.9}_{-3.4})\%$	

Mixing-Induced CP-Asymmetry

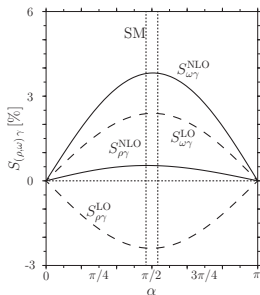
- Time-dependent CP-asymmetry in neutral B -meson decays involves the interference of $B^0 - \bar{B}^0$ mixing and decay amplitudes

$$a_{\text{CP}}^{\rho\gamma}(t) = \mathcal{A}_{\text{CP}}^{\text{dir}}(\rho^0\gamma) \cos(\Delta M_d t) + S_{\rho\gamma} \sin(\Delta M_d t)$$

- Mixing-induced CP-asymmetry is

$$S_{\rho\gamma} = \frac{2 \text{Im}(\lambda_{\rho\gamma})}{1 + |\lambda_{\rho\gamma}|^2}, \quad \lambda_{\rho\gamma} \equiv \frac{q}{p} \frac{A(\bar{B}_d^0 \rightarrow \rho^0\gamma)}{A(B_d^0 \rightarrow \rho^0\gamma)}$$

- In the SM, $q/p = e^{-2i\beta}$ to a good approximation
- Similar definitions can be written for $B^0 \rightarrow \omega\gamma$
- SM estimates: $S_{\rho\gamma}^{\text{NLO}} = (+0.5^{+4.1}_{-3.7})\%$ $S_{\omega\gamma}^{\text{NLO}} = (+3.8^{+4.4}_{-4.0})\%$
- Experimental value (657M) $S_{\rho\gamma}^{\text{Belle}} = (-83 \pm 65 \pm 18)\%$



Isospin-Violating Ratio

- Isospin-violating ratios in $B \rightarrow \rho \gamma$ decays are defined as

$$\Delta^{+0} = \frac{\Gamma(B^+ \rightarrow \rho^+ \gamma)}{2\Gamma(B^0 \rightarrow \rho^0 \gamma)} - 1 \quad \Delta^{-0} = \frac{\Gamma(B^- \rightarrow \rho^- \gamma)}{2\Gamma(\bar{B}^0 \rightarrow \rho^0 \gamma)} - 1$$

- Charged-conjugate averaged ratio

$$\Delta = \frac{1}{2} [\Delta^{+0} + \Delta^{-0}]$$

- In the leading order in α_s

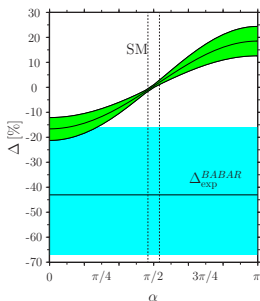
$$\Delta_{\text{LO}} = -2\epsilon_A^{(\pm)} |\lambda_u| \cos \alpha + (\epsilon_A^{(\pm)})^2 |\lambda_u|^2$$

- SM value is small [$\epsilon_A^{(\pm)} = 0.30 \pm 0.07$]

$$\Delta_{\text{th}}^{\text{SM}} = (0.7^{+1.8}_{-1.2})\% \quad \text{origine: } \alpha = (90 \pm 5)^\circ \quad [\text{PDG, 2010}]$$

- Current BABAR (465M) & BELLE (657M) measurements

$$\Delta_{\text{exp}}^{\text{BaBar}} = (-43^{+25}_{-22} \pm 10)\% \quad \Delta_{\text{exp}}^{\text{Belle}} = (-48^{+21+8}_{-19-9})\%$$



$SU(3)_F$ -averaged $B \rightarrow (\rho, \omega) \gamma$ Branching Ratio

- Definitions of the averaging procedures

$$\bar{B}(B \rightarrow \rho \gamma) \equiv \frac{1}{2} \mathcal{B}(B^+ \rightarrow \rho^+ \gamma) + \frac{\tau_{B^+}}{\tau_{B^0}} \mathcal{B}(B_d^0 \rightarrow \rho^0 \gamma)$$

$$\bar{B}[B \rightarrow (\rho, \omega) \gamma] \equiv \frac{1}{2} \left\{ \mathcal{B}(B^+ \rightarrow \rho^+ \gamma) + \frac{\tau_{B^+}}{\tau_{B^0}} [\mathcal{B}(B_d^0 \rightarrow \rho^0 \gamma) + \mathcal{B}(B_d^0 \rightarrow \omega \gamma)] \right\}$$

- Combinations of the branching fractions results

$$\bar{B}_{\text{th}}(B \rightarrow \rho \gamma) = (1.53 \pm 0.30) \times 10^{-6}$$

$$\bar{B}_{\text{th}}[B \rightarrow (\rho, \omega) \gamma] = (1.46 \pm 0.28) \times 10^{-6}$$

- Good agreement with experiment within current errors

Branching ratios (in units of 10^{-6}) [PDG, 2010]

Mode	BABAR (465M)	BELLE (657M)	Average [PDG]
$B \rightarrow \rho \gamma$	$1.73^{+0.34}_{-0.32} \pm 0.17$	$1.21^{+0.24}_{-0.22} \pm 0.12$	$1.39^{+0.22}_{-0.21}$
$B \rightarrow (\rho, \omega) \gamma$	$1.63^{+0.30}_{-0.28} \pm 0.16$	$1.14 \pm 0.20^{+0.10}_{-0.12}$	$1.30^{+0.18}_{-0.19}$

Summary

- Branching fractions of $B \rightarrow V \gamma$ (K^*, ρ, ω) predicted in the SM are in agreement with the experimental data within errors
- Charged-conjugate average, Δ , of the isospin-violating ratios for the decays $B \rightarrow \rho \gamma$ are found to be $|\Delta| \leq 3\%$ in the expected range of CKM parameters. Experimental measurements are not precise to test it
- Direct CP asymmetries in the $B \rightarrow (\rho, \omega) \gamma$ decays are close to 10% but uncertainties are rather large which requires further theoretical improvements
- Mixing-induced CP-asymmetry $S_{\rho \gamma}$ is highly suppressed in the $B^0 \rightarrow \rho^0 \gamma$ decay due to destructive interference of LO and NLO contributions. In the $B^0 \rightarrow \omega \gamma$ decay mode, $S_{\omega \gamma}$ is completely quantified and can be up to 10%

Backup Slides

$|V_{td}/V_{ts}|$ from $\bar{R}_{\text{exp}}[(\rho, \omega) \gamma / K^* \gamma]$ Ratio

- $|V_{td}/V_{ts}|$ can be extracted from [A. Ali & AP (2004)]

$$\bar{R}_{\text{exp}}[(\rho, \omega) \gamma / K^* \gamma] = \frac{\bar{B}_{\text{exp}}[B \rightarrow (\rho, \omega) \gamma]}{\bar{B}_{\text{exp}}(B \rightarrow K^* \gamma)} = r_{\text{th}}^{(\rho/\omega)} \left| \frac{V_{td}}{V_{ts}} \right|^2 \zeta_\rho^2$$

$$r_{\text{th}}^{(\rho/\omega)} = \frac{(M_B^2 - m_\rho^2)^3}{(M_B^2 - m_{K^*}^2)^3} [1 + \Delta R(\bar{\rho}, \bar{\eta}, \dots)] \simeq 0.984 \pm 0.075$$

- Using $\zeta_\rho = 0.86 \pm 0.07$ [Ball, Jones & Zwicky (2007)]

$$\bar{R}_{\text{exp}}^{\text{BELLE}} = 0.0284 \pm 0.0050_{-0.0029}^{+0.0027} \implies \left| \frac{V_{td}}{V_{ts}} \right| = 0.195_{-0.019}^{+0.020} \pm 0.015$$

$$\bar{R}_{\text{exp}}^{\text{BABAR}} = 0.039 \pm 0.008 \implies \left| \frac{V_{td}}{V_{ts}} \right| = 0.233_{-0.024}^{+0.025+0.022}_{-0.021}$$

- From ΔM_s measurements and Lattice-QCD

$$|V_{td}/V_{ts}| = 0.2060 \pm 0.0007(\text{exp})_{-0.0060}^{+0.0081}(\text{th}) \quad [\text{CDF Collab.}]$$

$$|V_{td}/V_{ts}| = 0.2018 \pm 0.0050(\text{exp})_{-0.0059}^{+0.0079}(\text{th}) \quad [\text{D0 Collab.}]$$

Experimental Data on $B \rightarrow K^* \gamma$ and $B \rightarrow X_s \gamma$ DecaysBranching ratios (in units of 10^{-6})

Quantity	BABAR	BELLE	CLEO	Average
$\mathcal{B}(B^+ \rightarrow K^{*+} \gamma)$	$42.2 \pm 1.4 \pm 1.6$	$42.5 \pm 3.1 \pm 2.4$	$37.6^{+8.9}_{-8.3} \pm 2.8$	42.1 ± 1.8
$\mathcal{B}(B^0 \rightarrow K^{*0} \gamma)$	$44.7 \pm 1.0 \pm 1.6$	$40.1 \pm 2.1 \pm 1.7$	$45.5^{+7.2}_{-6.8} \pm 3.4$	43.3 ± 1.5
$\mathcal{B}(B \rightarrow K^* \gamma)$	48.2 ± 1.5	42.7 ± 2.4	43.2 ± 6.2	46.5 ± 1.3
$\mathcal{B}(B \rightarrow X_s \gamma)$	$327 \pm 18^{+55}_{-41}$	$345 \pm 15 \pm 40$	$321 \pm 43^{+32}_{-29}$	$355 \pm 24 \pm 9$
$R(K^* \gamma / X_s \gamma)$	$0.147^{+0.028}_{-0.021}$	$0.131^{+0.015}_{-0.013}$	$0.135^{+0.033}_{-0.027}$	0.135 ± 0.011

$$\bar{\mathcal{B}}(B \rightarrow K^* \gamma) \equiv \frac{1}{2} \left[\mathcal{B}(B^+ \rightarrow K^{*+} \gamma) + \frac{\tau_{B^+}}{\tau_{B^0}} \mathcal{B}(B^0 \rightarrow K^{*0} \gamma) \right]$$

$$R(K^* \gamma / X_s \gamma) \equiv \frac{\bar{\mathcal{B}}(B \rightarrow K^* \gamma)}{\mathcal{B}(B \rightarrow X_s \gamma)}$$

Life-time ratio

$$\tau_{B^+} / \tau_{B^0} = 1.079 \pm 0.007$$